CORRELATION BETWEEN FORMULA WEIGHTS AND ABSOLUTE MOBILITIES
OBTAINED BY ISOTACHOPHORESIS FOR ALKYLAMMONIUM AND CARBOXYLATE IONS

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Absolute mobilities of n-alkylammonium, mono- and dicarboxylate ions were obtained by means of isotachophoresis. The mobilities were inversely proportional to the square roots of formula weights in the regions of ca. 60 to 130, ca. 70 to 160 and ca. 140 to 200 for the above ions, respectively.

It has been generally accepted that mobilities of ions can be described by Stokes' law, however, many of polyatomic ions deviate from the spherical form and may be regarded as prolate or oblate spheroids. Therefore, the simple hydrodynamic radius in Einstein-Stokes' equation cannot always be adopted for all of ions. In order to overcome this difficulty, many attempts have been made: Elworthy has evaluated the friction coefficients taking into account the spheroidal forms of $ions^{1)}$ and Edward and Waldron-Edward have proposed an empirical formula for evaluation of mobilities taking into account the spheroids and the increment of the Van der Waals radius by additional atoms and functional groups 2). the estimated values were not in good agreement with the observed ones in spite of taking careful account of several correction factors. On the other hand, Jokl3), Preetz and Blausius⁴⁾, and Kiso et al.⁵⁾ have shown that a simple correlation may exist between mobilities and formula weights for complex ions and a series of phosphoric acids, although the mobilities have been measured by the method of zone electrophoresis which included considerable uncertainties accompanied by adsorption, electroendosmosis, and difficulty in temperature control. Recently developed isotachophoresis 6), which has been used for the separation and analysis of ions with different effective mobilities, was expected to be more reliable in principle for evaluation of absolute mobilities in comparison with zone electrophoresis. The present method may have the following advantages even in comparison with the conductometric method: 1) Mobility of separated ion is obtained individually, 2) only small amount of sample is necessary, 3) several or more samples can be treated at once, 4) in other words, purification of sample is not necessary, and 5) in the aqueous system, purification of water is not necessary.

The isotachophoregram was obtained using a capillary type isotachophoretic analyzer (Shimadzu Seisakusho Ltd., Model IP-IB) equipped with a potential gradient detector (PGD). Since mobilities are sensitive to the change of temperature, the PGD cell was modified in order to measure the temperature of the migrating zones of separated ions during experiments. Figure 1 show a modified PGD cell. The thermo-detector was a polystyrene-molded copper-constantan thermocouple ($50\mu m$). The thickness and diameter of a disk were 0.4 and 4.5 mm, respectively, and the

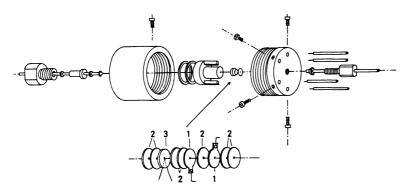


Fig. 1. Modified PGD cell.

- 1. Platinum electrodes
 (4.5mm x 0.1mm)
- 2. PTFE insulators (4.8mm x 0.1mm)
- 3. Thermo-detector

center of the disk was drilled with a hole $(0.5\text{mm}\ \phi)$. The conjunctive point of thermocouple was in direct contact with the electrolyte, so as to measure the temperature accurately. The output was connected to a battery-powered digital thermometer (Yokogawa Elec. Co., Ltd., Type 2575). Particular care was taken for the electric insulation of the cell, thermocouple and thermometer, since even slight leak current caused unstable isotachophoregram. The reading of the thermometer was calibrated against a standard thermometer. The error was within \pm 0.2 °C. A switch was added at the electrodes of PGD to short them and adjust null level of the potential gradient on a recorder. The switch was also effective for discharging the remained charges on the capillary system.

The leading and terminating solutions were aqueous imidazole-HCl and L-glutamic acid for the analysis of carboxylates and acetic acid-KOH and ϵ -aminocaproic acid for alkyl ammoniums. The concentrations of Cl and K were 0.005 mol/l and the pH of the leading electrolyte was adjusted to 7.0 and 4.84, respectively, in order to enforce the sample ions being in the full charged state. The length of the capillary tube (0.5mm i.d.) for separation was 20 cm and the applied current was varied in the region of 25 to 50 μ A so as not to exceed decomposition voltage at the electrodes of PGD. The voltage applied between the leading and terminating electrodes varied in the region of ϵa . 2 to 4kV at the initial state of migration.

The principle and mathematical treatment of isotachophoresis have been described previously 6). It should be noted that the ratio of the potential gradients of the sample or terminating zone (E_V) to the leading zone (E_L), E_V/E_L, is equal to the inverse ratio of the effective mobilities of the separated ions ($\bar{\mathbf{m}}_{V}$) to the leading ion ($\bar{\mathbf{m}}_{L}$);

 $E_V / E_L = \bar{m}_L / \bar{m}_V$

where we can obtain ${\rm E_V/E_L}$ values from the step heights of the recorder traces. The absolute mobilities of K⁺ and Cl⁻ ions have been extensively studied by the conductometric method⁷⁾ and the temperature dependence of them can be written as;

$$m_0(K^+) = (1.361 t + 41.701) x 10^{-5} cm^2/Vs$$

 $m_0(C1^-) = (1.471 t + 42.301) x 10^{-5} cm^2/Vs$,

where t denotes the temperature in centigrade. These values were corrected to the effective mobilities at the finite concentration of 0.005 mol/l by the use of Onsager's equation. Then, we can obtain effective mobilities of sample ions $\bar{\mathbf{m}}_V$. In order to convert $\bar{\mathbf{m}}_V$ to absolute mobility, the calculated ionic strength at the isotachophoretic equilibrium was employed. In practice, a computer program of

least-squares method was used for the evaluation of absolute mobility. All calculations were carried out using a computer system HITAC 8700/8800 of Hiroshima University.

All samples were commercial products purchased from Tokyo Kasei Co., Ltd. Imidazole was purified by repeated recrystallization from benzene solution, since slight anionic impurity was found.

The estimation of mobility by the present method seemed reliable taking into account the fact that the obtained absolute mobility of acetate ion well agreed with that obtained by conductometric method. Namely, the extensive works 7) gave the temperature dependence of absolute mobility of acetate ion as follows;

$$m_0(Ac^-) = (0.800 t + 22.14) x 10^{-5} cm^2/Vs.$$

This equation gives m_0^0 at 20.6°C as 38.6 x 10^{-5} and the value obtained by isotachophoresis was 37.9 x 10^{-5} cm²/Vs. The discrepancy was 0.7 x 10^{-5} , within the experimental error of the present method, \pm 0.8 x 10^{-5} . The error was estimated from the reproducibility for E_V/E_L values of \pm ea. 0.04.

Table 1 listed the observed $\rm E_V/E_L$ at 21.4 ± 0.5°C, the calculated values of $\rm E_V/E_L$, pH of zones, concentrations of sample and buffer ions, effective and absolute mobilities for n-alkylammonium ions. Figure 2 shows the correlation between absolute mobilities ($\rm m_0$) and the inverse of square roots of formula weights (1/ $\rm \sqrt{FW}$) for n-alkylammonium ions at 21.4 and 9°C. Figure 3 shows the correlation for mono- and dicarboxylates at 20.6°C. For dicarboxylate ions, the relation of $\rm m_0$ vs. 1/ $\rm \sqrt{FW/2}$ was also given in order to show the difference of mobilities due to net charges between mono- and dicarboxylate ions. It is apparent that $\rm m_0$ and 1/ $\rm \sqrt{FW}$ correlated linearly in the regions of formula weights of 60 to 130 for n-alkylammoniums, 73 to 157 and 144 to 200 for mono- and dicarboxylates, respectively, although the linear correlation was not held for the relatively small ions (FW <60-70). Figure 4 shows the extensive works on the mobilities of alkylammonium ions $\rm ^{7}$) with the formula weights of 74 to 256 at 25 and 18°C. As expected, the linearity of $\rm m_0$ vs. 1/ $\rm ^{7}\rm FW$ was confirmed. It should be noticed that the linear correlation of primary and secondary ammonium ions differs from that of tertiary

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Ionic species	_{FW} a)	Obsd	Calc	d pH	C _A b)	c _B c)	md)	m ₀ e)
methylammonium	32.1	1.296 1.295	1.294 1.29	5 4.799	4.489	4,506	52.23	55.0
ethylammonium	46.1	1.601 1.595	1.602 1.59	9 4.739	4.054	4.073	42.29	44.8
n-propylammonium	60.1	1.929 1.945	1.924 1.93	3 4.696	3.658	3.679	35.00	37.3
n-butylammonium	74.1	2.067 2.094	2.103 2.08	8 4.673	3.496	3.517	32.40	34.6
n-amylammonium	88.2	2.223 2.211	2.266 2.23	3 4.653	3.354	3.376	30.29	32.4
n-hexylammoinium	102.2	2.392 2.347	2.379 2.37	2 4.633	3.227	3.250	28.51	30.6
n-octylammonium	130.3	2.614 2.632	2.595 2.61	4 4.600	3.024	3.049	25.88	27.8

Table 1. Observed $\mathrm{E_{V}/E_{I}}$ and calculated mobilities of n-alkylammonium ions.

a) Formula weights, b) Concentrations of samples (mmol/l), c) Concentrations of buffer (mmol/l), d) Effective mobilities of sample ions $(10^{-5} \text{cm}^2/\text{Vs})$, and e) Absolute mobilities $(10^{-5} \text{cm}^2/\text{Vs})$.

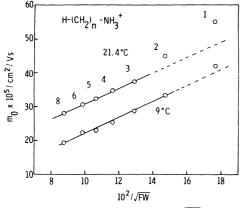


Fig. 2. $m_0 vs. 1/\sqrt{FW}$ of n-alkylammonium ions.

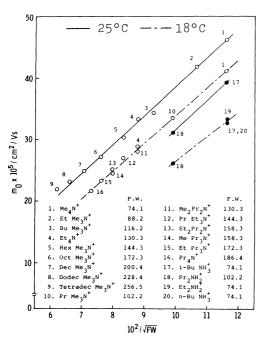


Fig. 4. $m_0 \ vs. \ 1/\sqrt{FW}$ of alkylammonium ions.

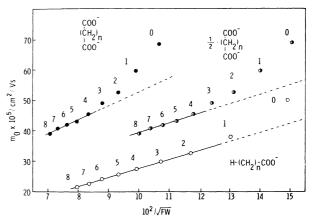


Fig. 3. $m_0 vs. 1/\sqrt{FW}$ of mono- and dicarboxylate ions (20.6°C).

and quarternary ammonium ions. These facts suggested that the absolute mobilities of alkylammonium and carboxylate ions can be estimated from the formula weights and their structures. For the larger ions, although the present experiments were limited due to the solubility of samples in water, the use of mixed solvents may afford more detailed relation between \mathbf{m}_0 and formula weights and practical equations for evaluation of \mathbf{m}_0 of non-spherical ions will be described.

Since the temperature of the present experimental system was governed by a room temperature, more accurate values of m₀ are expected, if it is controlled precisely. Construction of temperature control system for whole capillary system is now in progress and a study on the temperature dependence of mobility is also in progress.

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